

Momentum

$$p = mv$$

$$m = 220 \text{ kg} \quad v = 8.00 \text{ m/s}$$

$$p = mv = (220 \text{ kg})(8.00 \text{ m/s}) = 1760 \text{ kg m/s}$$

Thought experiment

Bullet $m = 0.015 \text{ kg} \quad v = 900 \text{ m/s}$

Football player $m = 103.9 \text{ kg} \quad v = 8.34 \text{ m/s}$

Momentum of bullet: $p = mv = (0.015 \text{ kg})(900 \text{ m/s}) = 13.5 \text{ kg m/s}$

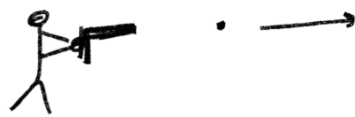
Momentum of player: $p = mv = (103.9 \text{ kg})(8.34 \text{ m/s}) = 866.5 \text{ kg m/s}$

Momentum is conserved.

Person

$$m_1 = 80 \text{ kg}$$

What is the velocity of the recoil?



Bullet

$$m_2 = 0.040 \text{ kg}$$

$$v_2 = 1200 \text{ m/s}$$

$$\frac{m_1 v_1}{m_1} = \frac{m_2 v_2}{m_1}$$

$$v_1 = \frac{m_2 v_2}{m_1} = \frac{(0.040 \text{ kg})(1200 \text{ m/s})}{80 \text{ kg}}$$

$$= \boxed{0.6 \text{ m/s}}$$

Elastic collision — kinetic energy and momentum is conserved.

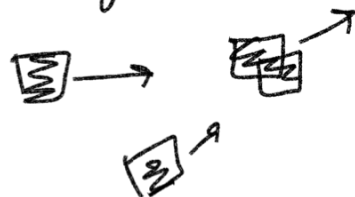
$$M_1 v_{1i} + M_2 v_{2i} = M_1 v_{1f} + M_2 v_{2f}$$

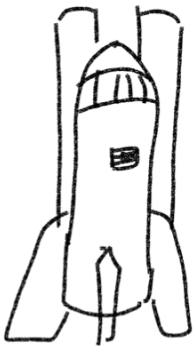
Only exists with molecules

Perfectly Inelastic Collisions

Two masses collide and form a single mass.

$$m_1 v_1 + m_2 v_2 = (m_1 + m_2) v_f$$





$$m_1 = 2,030,000 \text{ kg}$$

$$v_1 = \textcircled{+} 8,000 \text{ m/s}$$

space shuttle



$$m_2 = 550,000 \text{ kg}$$

$$v_2 = -1,000 \text{ m/s}$$

Nate's tombstone

$$\frac{m_1 v_1 + m_2 v_2}{(m_1 + m_2)} = \frac{(m_1 + m_2) v_f}{(m_1 + m_2)}$$

$$v_f = \frac{m_1 v_1 + m_2 v_2}{(m_1 + m_2)} = \frac{(2,030,000 \text{ kg})(8,000 \text{ m/s}) + (550,000 \text{ kg})(-1,000 \text{ m/s})}{2,030,000 + 550,000}$$
$$= \boxed{6081.4 \text{ m/s}}$$

BLIMP



$$m_1 = 5,824 \text{ kg}$$

$$v_1 = 15.65 \text{ m/s}$$

vs.

CHARTER

BUS

(Full)



$$m_2 = 20,139 \text{ kg}$$

$$v_2 = 31.3 \text{ m/s}$$

x-direction

Blimp

$$p = m_1 v_1$$

$$(5,824 \text{ kg})(15.65 \text{ m/s})$$

$$= 91,145.6 \text{ kg m/s}$$

y-direction

Bus

$$p = m_2 v_2$$

$$(20,139 \text{ kg})(31.3 \text{ m/s})$$

$$= 630,351 \text{ kg m/s}$$

$$r = \sqrt{x^2 + y^2} = \sqrt{(91,145.6)^2 + (630,351)^2} =$$

$$\text{tot momentum} = 636,906 \text{ kg m/s}$$

$$\text{resulting velocity} = \frac{\text{tot. momentum}}{\text{tot. mass}} = \frac{636,906 \text{ kg m/s}}{(5,824 + 20,139) \text{ kg}} = 24.5 \text{ m/s}$$

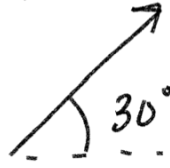
$$\theta = \tan^{-1} \frac{y}{x} = \tan^{-1} \left(\frac{630,351}{91,145.6} \right) = 81.8^\circ$$

$$\boxed{24.5 \text{ m/s}, 81.8^\circ}$$



Density of Potato $\rightarrow 159 \text{ g/metric cup}$
 $1000 \text{ ft}^3 \rightarrow \text{met}_{\text{cup}}$

$$D = \frac{M}{V} \quad M = DV$$



Frankie D'
/Cool.

Mr. Potato Head

$$m_1 = 6,080 \text{ kg}$$

$$v_1 = 17.9 \text{ m/s}$$

X-momentum

$$\text{PH} \quad (6080 \text{ kg})(17.9 \text{ m/s})$$

$$108,832 \text{ kg m/s}$$

$$\text{FDK} \quad (13,227)(4.98) \cos 30$$

$$57,045 \text{ kg m/s}$$

$$\text{Tot} \quad 165,877 \text{ kg m/s}$$

Kool-Aid Man

$$m_2 = 13,227 \text{ kg}$$

$$v_2 = 4.98 \text{ m/s}$$

y-momentum

0

$$(13,227)(4.98) \sin 30$$

$$32,935 \text{ kg m/s}$$

$$32,935 \text{ kg m/s}$$

total momentum $\sqrt{x^2 + y^2} = \sqrt{(165,877)^2 + (32,935)^2}$

$$\theta = \tan^{-1} \left(\frac{32,935}{165,877} \right)$$

$$\theta = 11.2^\circ$$

$$= \frac{169,115 \text{ kg m/s}}{6080 + 13227} = 8.8 \text{ m/s}$$

$$\boxed{8.8 \text{ m/s}, 11.2^\circ}$$

