

Find the opposite reciprocal.

a) 8 $\xrightarrow{\text{opp}} -8 \xrightarrow{\text{rec}} \boxed{-\frac{1}{8}}$

b) $-\frac{4}{3} \xrightarrow{\text{opp}} \frac{4}{3} \xrightarrow{\text{rec}} \boxed{\frac{3}{4}}$

Rational

number that can be put into a fraction

Irrational

number that cannot be put into a fraction.

Rational Numbers

Counting Numbers - 1, 2, 3, 4, 5, ...

whole Numbers - 0, 1, 2, 3, 4, 5, ...

Integer - All whole numbers and their opposites

..., -3, -2, -1, 0, 1, 2, 3, ...

$$0.45 \square \text{ terminal decimal} \quad \frac{45 \div 5}{100 \div 5} = \frac{9}{20} \text{ Rational}$$

$$0.\bar{4}444\dots = \frac{4}{9} \quad \text{single repeating - Rational decimal}$$

$$0.3333\dots = \frac{3 \div 3}{9 \div 3} = \frac{1}{3}$$

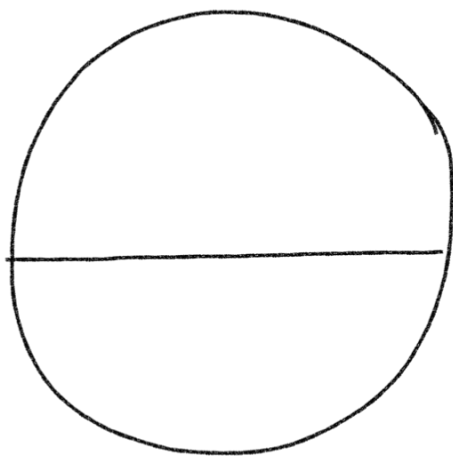
$$0.\overline{234}234\overline{234}\dots \quad \frac{234}{999} \quad \text{group repeating - Rational decimal}$$

$$0.12444\dots = 0.12\bar{4} \quad \text{repeating decimal - Rational}$$

0.123456\dots \quad \text{irrational - no repeat.}

π - pi irrational number

3.141592\dots



π represents the number of times the diameter can be wrapped around a circle.

$$C = \pi d \quad \pi = \frac{C}{d} \rightarrow \text{irrational} \dots ?$$

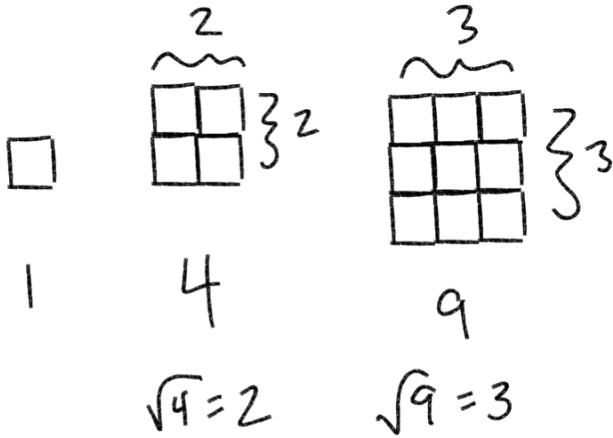
Rational Numbers

Perfect Square

$$\sqrt{36} = \pm 6$$

$$6 * 6 = 36$$

$$-6 * -6 = 36$$



Consecutive Perfect Squares
odd numbers

$$1 \quad \sqrt{0} = 0$$

$$3 \quad \sqrt{1} = \pm 1$$

$$5 \quad \sqrt{4} = \pm 2$$

$$7 \quad \sqrt{9} = \pm 3$$

$$9 \quad \sqrt{16} = \pm 4$$

$$11 \quad \sqrt{25} = \pm 5$$

$$13 \quad \sqrt{36} = \pm 6$$

$$15 \quad \sqrt{49} = \pm 7$$

$$17 \quad \sqrt{64} = \pm 8$$

$\sqrt{40}$ not a perfect square
irrational

- 1.) 4 Rational
Counting, whole, integer
- 2.) -7 Rational
integer
- 3.) 0.8888... Rational
repeating
- 4.) 0.143143 \square Rational
terminal
- 5.) 0.347348... irrational
- 6.) 0.428428... Rational
repeating
- 7.) $\sqrt{81}$ Rational
perfect square
- 8.) $\sqrt{200}$ irrational

Commutative Property

$$8 + 3 = 3 + 8$$

$$11 = 11$$

$$8 * 3 = 3 * 8$$

$$24 = 24$$

Add/Mult order does not matter

Associative Property

$$(3 + 4) + 5 = 3 + (4 + 5)$$

$$7 + 5 = 3 + 9$$

$$12 = 12$$

$$(3 * 4) * 5 = 3 * (4 * 5)$$

$$12 * 5$$

$$60 = 60$$

$$3 * 20$$

You can shift parentheses when you are all adding or multiplying.

Identity Property

Add: $3 + 0 = 3$

$$a + 0 = a$$

Mult: $3 * 1 = 3$

$$a * 1 = a$$

Inverse Property

Add: $4 + (-4) = 0$

$$a + (-a) = 0$$

Add opposites = 0


Mult: $4 * (\frac{1}{4}) = 1$

$$a * \frac{1}{a} = 1 \quad a \neq 0$$

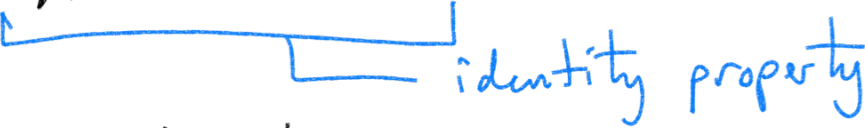
Mult by inverses = 1

$$x + 4 = 5$$
$$\quad -4 \quad -4$$

$$x + 4 + (-4) = 5 + (-4)$$


inverse property

$$x + 0 = 5$$


identity property

$$x = 5$$

Distributive Property

$$4(5+3) = 4(5) + 4(3)$$
$$4(8) = 20 + 12$$
$$32 = 32$$

Needham Slap!

$$3(a+b)$$
$$3a + 3b$$

$$1.) \quad a = b + 0$$

identity

$$2.) \quad 5(a - bc) = 5a - 5bc$$

distributive

$$3.) \quad c + (-c) = 0$$

inverse

$$4.) \quad a + (b + c) = (a + b) + c$$

associative

$$5.) \quad abc = cab$$

commutative

$$a * b * c = c * a * b$$

Algebraic Expressions \rightarrow No equal sign!

$$(4x + 1) + 2x$$

$$x = 3$$

Substitute

$$\begin{array}{ccc} \downarrow & & \downarrow \\ (4(3) + 1) + 2(3) & & \end{array}$$

Input $\rightarrow 3$

$$(12 + 1) + 2(3)$$

Output $\rightarrow 19$

$$13 + 6 = \boxed{19}$$

$$6p^2 - (3p^2 + 2q^2)$$

$$p = 1 \quad q = 5$$

$$\downarrow$$
$$6(1)^2 - (3(1)^2 + 2(5)^2)$$

$$6(1) - (3(1) + 2(25))$$

$$6 - (3 + 50)$$

$$6 - 53 = -47$$

Follow
PEMDAS!

output $\rightarrow -47$

$$2(m - n^2) - 6(n^2 + 3m)$$

"simplify"

$$2m - 2n^2 - 6n^2 - 18m$$

$$2m - 18m \quad -2n^2 - 6n^2$$

$$\boxed{-16m \quad -8n^2}$$

combine like
terms