

$$(2i+3)(4i-5)$$

$$8i^2 - 10i + 12i - 15$$

$$8(-1) - 10i + 12i - 15$$

$$(-8) + 2i(-15)$$

$$\boxed{-23 + 2i}$$

↑ real ↑ imaginary

FOIL

$$i^2 = i \cdot i = -1$$

$$\downarrow$$

$$\sqrt{-1} \cdot \sqrt{-1} = -1$$

$$\sqrt{4} \cdot \sqrt{4} = \sqrt{16} = 4$$

$$\sqrt{4} \cdot \sqrt{4} = 4$$

$$\sqrt{7} \cdot \sqrt{7} = 7$$

$$-8 - 15$$

$$-8 + (-15)$$

$$-23$$

$$(8-3i)(4+2i)$$

$$32 + 16i - 12i - 6i^2$$

$$\downarrow$$

$$32 + 16i - 12i + 6$$

$$\boxed{38 + 4i}$$

$$-6i^2$$

$$\downarrow$$

$$-6(-1) = +6$$

$$x^2 + 20x + 75 = 0$$

Quadratic Formula

$$1.) h = \frac{-b}{2a}$$

$$a = 1 \quad b = 20 \quad c = 75$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

h

Discriminant

$$h = \frac{-b}{2a} = \frac{-20}{2(1)} = \frac{-20}{2} = -10 \quad h = -10$$

to find k...

vertex (-10, -25)

$$\underline{k} = (-10)^2 + 20(-10) + 75$$
$$100 - 200 + 75 = -100 + 75 = -25 = k$$

2.) Find the zeros → take the average

$$x^2 + 20x + 75 = 0$$

$$\underline{15} * \underline{5} = 75$$

$$(x + 5)(x + 15) = 0$$

$$\underline{15} + \underline{5} = 20$$

$$\begin{array}{cc} \downarrow & \downarrow \\ -5 & -15 \end{array}$$

Average of zeros

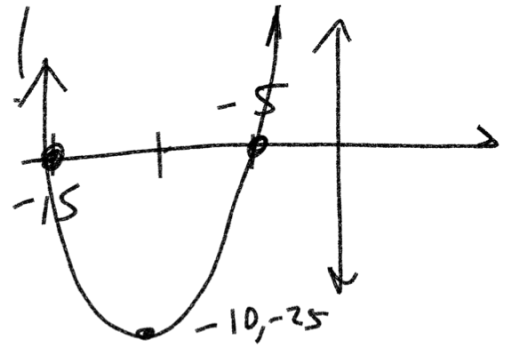
$$h = \frac{-15 + (-5)}{2} = \frac{-20}{2} = (-10)$$

$$k = (-10 + 5)(-10 + 15)$$
$$(-5)(5) = -25$$

vertex: (-10, -25)

Completing the Square

↙ "a"
 $x^2 + 20x + 75 = 0$



$$(x^2 + 20x) + 75 = 0$$

$b = 20$
 $(\frac{20}{2})^2 = 10^2 = 100$

↑ +100 -100 ↑

1.) 2020 it

2.) factor out "a" term

3.) $(\frac{b}{2})^2$ add inside sub outside

$$(x^2 + 20x + 100) + 75 - 100$$

4.) square root first and last

$$(x^2 + 20x + 100) - 25$$

vertex form

$\sqrt{x^2}$ ↓ ↓ ↓ $\sqrt{100}$

$$(x + 10)^2 - 25$$

$$y = a(x - h)^2 + k$$

opposite ↓ ↓

vertex

$$(-10, -25)$$

$$(x + 10)^2 = (x + 10)(x + 10)$$

$$x^2 + 10x + 10x + 100$$

$$x^2 + 20x + 100$$

$$x^2 + 16x + 48 = 0$$

Convert to vertex form.

$$\left(x^2 + 16x \right) + 48 = 0$$

\uparrow \uparrow

$$\left(\frac{16}{2} \right)^2 + 64 - 64$$

$$8^2 = 64$$

1.) 2020 it.

2.) factor out "a"

3.) $\left(\frac{b}{2} \right)^2 \rightarrow$ add inside
sub outside

4.) Square root the
first and last

$$(x^2 + 16x + 64) + 48 - 64$$

$$(x^2 + 16x + 64) - 16$$

$\sqrt{x^2}$ \downarrow \downarrow \downarrow $\sqrt{64}$

$$(x + 8)^2 - 16$$

vertex: (h, k)

$(-8, -16)$

Find zeros

$$\Downarrow$$
$$(x + 8)^2 - 16 = 0$$

+16 +16

$$\sqrt{(x + 8)^2} \neq \sqrt{16}$$

$$x + 8 = \pm 4$$

-8 -8

$$\sqrt{16} = \pm 4$$

$$x = -8 \pm 4$$

$$-8 + 4$$

(-4)

$$-8 - 4$$

(-12)

$$2x^2 + 8x + 6 = 0$$

$$\left(2x^2 + 8x\right) + 6 = 0$$

1.) 2020 it

2.) factor out "a"

3.) $\left(\frac{b}{2}\right)^2$

$$2(x^2 + 4x) + 6 = 0$$

$$\left(\frac{4}{2}\right)^2$$

$$+4$$

$$-4(2)$$

"a"

$$2^2 = 4$$

$$2(x^2 + 4x + 4) + 6 - 8$$

$$2(x^2 + 4x + 4) - 2$$

$$\sqrt{x^2}$$

$$\downarrow$$

$$\downarrow$$

$$\sqrt{4}$$

$$2(x+2)^2 - 2$$

vertex: $(-2, -2)$