

Algebra 2 Chapter 5 Pre-Test

- 1.) (5 pts total, 2.5 pts each) Rewrite each function in standard form. Indicate whether the function is a quadratic.

a) $(x - 7)(x - 7)$

$$x^2 - 7x - 7x + 49$$

$$\boxed{x^2 - 14x + 49}$$

b) $2(x + 2)^2 - 2x^2$

1.) Highest exponent
is x^2

2.) All exponents must
be whole numbers—
No negatives or
fractions/decimals

- 2.) (5 pts) Find a quadratic model for the following set of values:

$(-4, 8), (-1, 5), (1, 13)$

$$(-4, 8) \quad y = Ax^2 + Bx + C$$

$$f(-4) = 8 \quad 8 = A(-4)^2 + B(-4) + C$$

$$\textcircled{1} \quad 8 = 16A - 4B + C$$

$$(-1, 5) \quad y = Ax^2 + Bx + C$$

$$5 = A(-1)^2 + B(-1) + C$$

$$(1, 13) \quad \textcircled{2} \quad 5 = A - B + C$$

$$y = x^2 + 4x + 8$$

$$y = Ax^2 + Bx + C$$

$$\begin{aligned} 13 &= A(1)^2 + B(1) + C \\ 13 &= A + B + C \end{aligned}$$

$$(1, 13) \quad 13 = A(1)^2 + B(1) + C$$

$$\textcircled{3} \quad 13 = A + B + C$$

$$-5 = -A + B - C$$

$$13 = A + B + C$$

$$\frac{8}{2} = \frac{2B}{2} \quad \boxed{B = 4}$$

$$\textcircled{1} \quad 8 = 16A - 4B + C$$

$$\textcircled{2} \quad 5 = \boxed{A} - B + C$$

$$\textcircled{3} \quad 13 = \boxed{A} + B + C$$

$$\textcircled{1} \quad 8 = 16A - 4(4) + C$$

$$8 = 16A - 16 + C$$

$$+16 \qquad +16$$

- 3.) (10 pts total, 5 pts each) Graph each parabola. Label the vertex and axis of symmetry

$$\textcircled{a} \quad x^2 - 4x + 10$$

$$13 = A + B + C$$

$$13 = 1 + 4 + C$$

$$13 = 5 + C$$

$$-5 = -C$$

$$\boxed{C = 8}$$

$$\text{vertex: } (h, k) \quad y = \text{int } h$$

$$h = \frac{-b}{2a} = \frac{-(-4)}{2(1)} = 2$$

$$\frac{4}{2} = 2 = h$$

$$-b \pm \sqrt{b^2 - 4ac}$$

$$2a$$

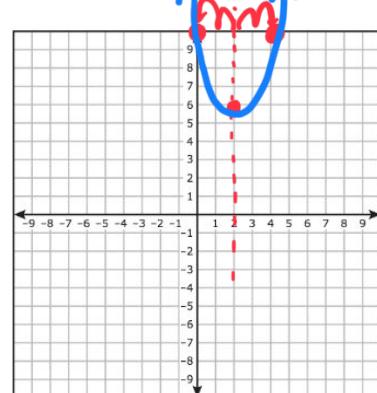
$$k = (2)^2 - 4(2) + 10$$

$$\frac{4 - 8 + 10}{-4 + 10} = 6$$

$$\text{Vertex: } (2, 6)$$

$$\text{axis of symmetry} \quad x = h$$

$$x = 2$$



$$\textcircled{3} \quad 13 = A + 4 + C$$

$$-4 - 4$$

$$13 = A + C$$

$$24 = 16A + C$$

$$-(9 = A + C)$$

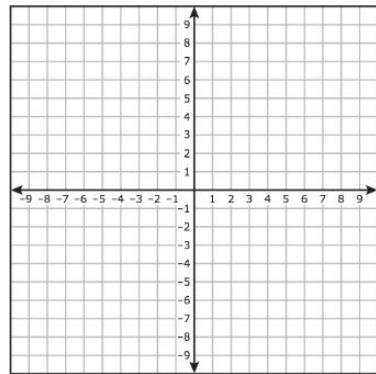
$$24 = 16A + C$$

$$-9 = -A - C$$

$$\boxed{A = 1}$$

$$\frac{15}{15} = \frac{15A}{15}$$

b) $2x^2 + 12x + 17$



4.) (20 pts total, 5 pts each) Factor each expression.

a) $x^2 + 5x - 14$

$$\begin{array}{l} 7 * -2 = -14 \\ 1 + -2 = 5 \end{array} \quad \left. \begin{array}{l} 7 \\ 1 \end{array} \right\} \quad \left. \begin{array}{l} -2 \\ -2 \end{array} \right\}$$

$$(x+7)(x-2)$$

b) $x^2 + 7x + 12$

c) $2x^2 + 13x + 15$

$$\frac{2}{2 \cdot 1}$$

$$\frac{15}{1 \cdot 15} \quad \left. \begin{array}{l} 15 \\ 1 \end{array} \right\} \quad \left. \begin{array}{l} 15 \\ 15 \end{array} \right\} \quad \frac{3}{3 \cdot 5} \quad \left. \begin{array}{l} 3 \\ 3 \end{array} \right\}$$

$$(x-5)(2x-3)$$

$$\begin{array}{r} 2x - 1 \\ \times \quad 2x^2 - x \\ \hline -15 \quad -30x \quad 15 \\ -30x + (-x) \\ \hline -31x \end{array}$$

$$\begin{array}{r} 2x - 15 \\ \times \quad 2x^2 - 15x \\ \hline -1 \quad -2x \quad 15 \\ -15x + (-2x) \\ \hline -17x \end{array}$$

$$\begin{array}{r} 2x - 3 \\ \times \quad 2x^2 - 3x \\ \hline -5 \quad -10x \quad 15 \\ -10x + (-3x) \\ \hline -13x \end{array}$$

$$\begin{array}{r} 2x - 5 \\ \times \quad 2x^2 \\ \hline -3 \quad 15 \end{array}$$

c) $2x^2 - 13x + 15$

d) $\frac{3x^2 - 5x - 12}{}$

$a=2 \quad b=-13 \quad c=15$

$$\begin{array}{r} x=5 \\ -5 \end{array}$$

$$\begin{array}{r} x=\frac{3}{2} \\ -\frac{3}{2} \end{array}$$

$$x-5=0 \quad x-\frac{3}{2}=0$$

Quadratic formula

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\frac{-(-13) \pm \sqrt{(-13)^2 - 4(2)(15)}}{2(2)}$$

5.) (10 pts total, 2.5 pts each) Evaluate the discriminant of the equation. Indicate the number of real roots for each.

a) $x^2 - 4x + 4$ factored

b) $-2x^2 + 6x - 14$

$$2(x-\frac{3}{2})(2x-3)$$

c) $x^2 + 9x + 18$

$$\frac{13 \pm \sqrt{169 - 120}}{4}$$

$$\frac{13 \pm \sqrt{49}}{4} = \frac{13 \pm 7}{4}$$

$$\frac{13+7}{4} = \frac{20}{4} = 5$$

$$\frac{13-7}{4} = \frac{6}{4} = \frac{3}{2}$$

d) $2x^2 + 11x - 21$

6.) (15 pts total, 7.5 pts each) Solve using the Quadratic Equation.

a) $x^2 = 3x + 2$

b) $3x^2 - 5x = -12$

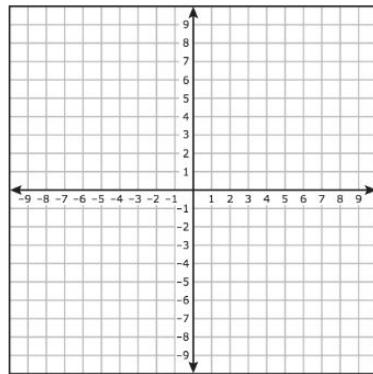
7.) (15 pts total, 7.5 pts each) Place each equation in vertex form by completing the square.
Please show all your work.

a) $x^2 = 5x + 14$

b) $2x^2 + 6x - 7 = 0$

8.) (20 pts total, 10 pts each) Graph each equation completely. Plot all roots, intercepts, and the vertex.

a) $x^2 + 6x + 9$



b) $x^2 - 4x - 5$

